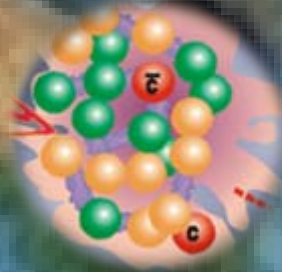


# Quark-Gluon Plasma and Relativistic Heavy Ion Collisions



**G.Zinovjev**

Bogolyubov Institute for Theoretical Physics, Kiev, UKRAINE

June 23-25, Bautzen,

# High energy density physics

## E.Teller, Ya.Zeldovich

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### REMINDER: WHAT'S A PLASMA?

- ✗ 4<sup>th</sup> state of matter (after solid, liquid and gas)
- ✗ a plasma is:
  - + ionized gas which is macroscopically neutral
  - + exhibits collective effects
- ✗ interactions among charges of multiple particles
  - + spreads charge out into characteristic (Debye) length,  $l_D$
  - + multiple particles inside this length
  - + “normal” plasmas are electromagnetic
  - + quark-gluon plasma interacts via strong interaction
    - ✗ color forces rather than EM
    - ✗ exchanged particles: gluon instead of photon

classical electromagnetic plasma can be a good liquid too if sufficiently strongly coupled

$$\Gamma = Q^2 / dT$$

**Coulomb coupling parameter**

( $T$  – plasma temperature,  $d$  – interparticle distance,  $Q$  – charge of plasma particles)

one-component plasma with pure Coulomb interaction this parameter corresponds to ratio of interaction energy to thermal energy per particle

most plasmas in nature and laboratory are weakly coupled  
(could be a gas, liquid, and even solid phase)

$\Gamma > 1$  behaves like a liquid

$\Gamma > 172$  plasma particles are predicted to arrange in ordered structures  
(the plasma crystal) was discovered in dusty plasmas

in real plasmas

Coulomb interactions modified to Yukawa because of screening

$\Gamma$  is not above ratio

additional parameter is of importance  $\kappa = d/\lambda_D$

$\lambda_D$  – Debye screening length,  $\kappa \gg 1$  means plasma is weakly coupled

( $\Gamma$ -  $\kappa$ )-plane defines the phase structure

1. Astrophysical Phenomena
2. Astro Fundamental Physics

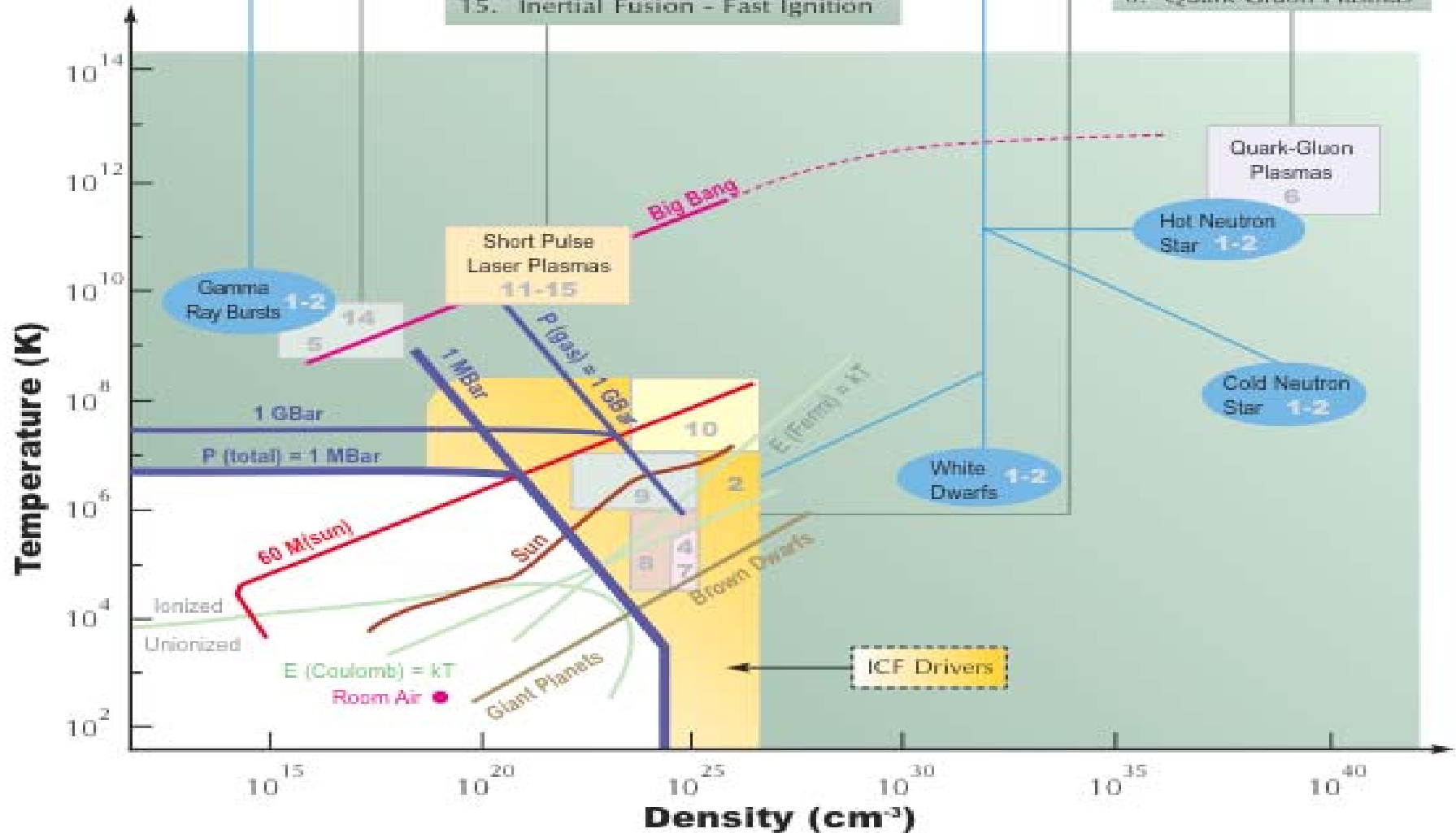
UBIQUITOUS

5. Plasma Wakefield Accelerators

11. Relativistic Matter
12. Attosecond Dynamics
13. Ultra-fast X-ray Science
14. Laser Acceleration of Particles
15. Inertial Fusion - Fast Ignition

3. Lab Astrophysics
4. Heavy Ion-Driven HEDP
7. Warm Dense Matter
8. Compressible Dynamics
9. Radiative Hyrdodynamics
10. Inertial Confinement Fusion (ICF)

6. Quark-Gluon Plasmas





# Multiparticle Production at High Energies

## Statistical approach



**E. Fermi, 1950**

$$V_n = (\gamma V_0)^{n-1}, \quad V_0 = (4/3) \pi (1/m_\pi)^3$$

$\gamma$  - Lorentz factor,  $m_\pi$  -  $\pi$ -meson mass

proposed strong interaction leading to equilibration:  $\langle n \rangle \sim s^{1/4}$



**I. Pomeranchuk,  
1951**

$$V_n = (n \gamma V_0)^{n-1} \quad \text{introduced freezeout}$$



**L. Landau, 1953**

explained that one should use hydro  
in between, saving the Fermi's prediction  
via entropy conservation



**R. Hagedorn,  
1965**

$$\rho(m) \sim m^{-a} \exp(bm), \quad b = 1/T_0, \quad T_0 \sim m\pi$$

$T_0$  - ultimate temperature



**K. Huang,  
S. Weinberg, 1971**

Fourth law of thermodynamics,  
ultimate temperature

# Space-Time Picture:

Early work on  
energy densities:

Shuryak 1974

Zinovjev et al  
1974

Ansiehtty et. al.  
1980

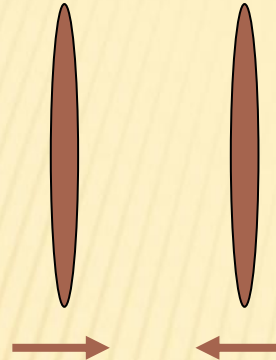
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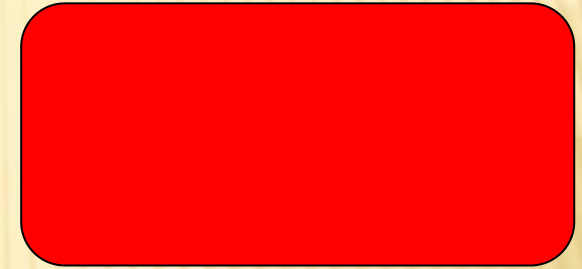
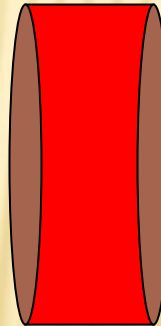
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Colliding  
Nuclei

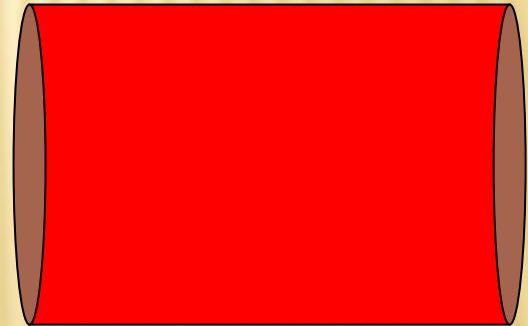
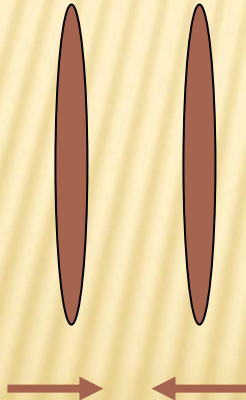


Collision



Landau Hydrodynamics

Expanding Fireball



Longitudinal flow

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are needed to see this picture.

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are needed to see this picture.

Landau  
Feynman  
Bjorken

Bjorken Hydrodynamics

- ✖ **hadrons have an intrinsic size with a radius  $r_h \approx 1\text{fm}$  and hence a hadron needs a space of volume  $V_h \approx (4\pi / 3)r_h^3$  in order to exist, it suggests a limiting density  $n_c = 1/V_h \approx 24\text{fm}^{-3}$  of hadronic matter, beyond this point hadrons overlap more and more, so that eventually they cannot be identified any more.**
- ✖ **hadronic interactions provide abundant resonance production, and the resulting number  $\rho(m)$  of hadron species increases exponentially as function of the resonance mass  $m$ ,  $\rho(m) \approx \exp(b m)$  such a form for  $\rho(m)$  appeared first in statistical bootstrap model based on self-similar resonance formation or decay, then also obtained in more dynamical dual resonance approach which specifies the scattering matrix through its pole structure. In hadron thermodynamics the exponential increase of the resonance degeneracy is found to result in an upper limit for the temperature of hadronic matter,**  

$$T_c = 1 / b \approx 150 - 200 \text{ MeV}.$$



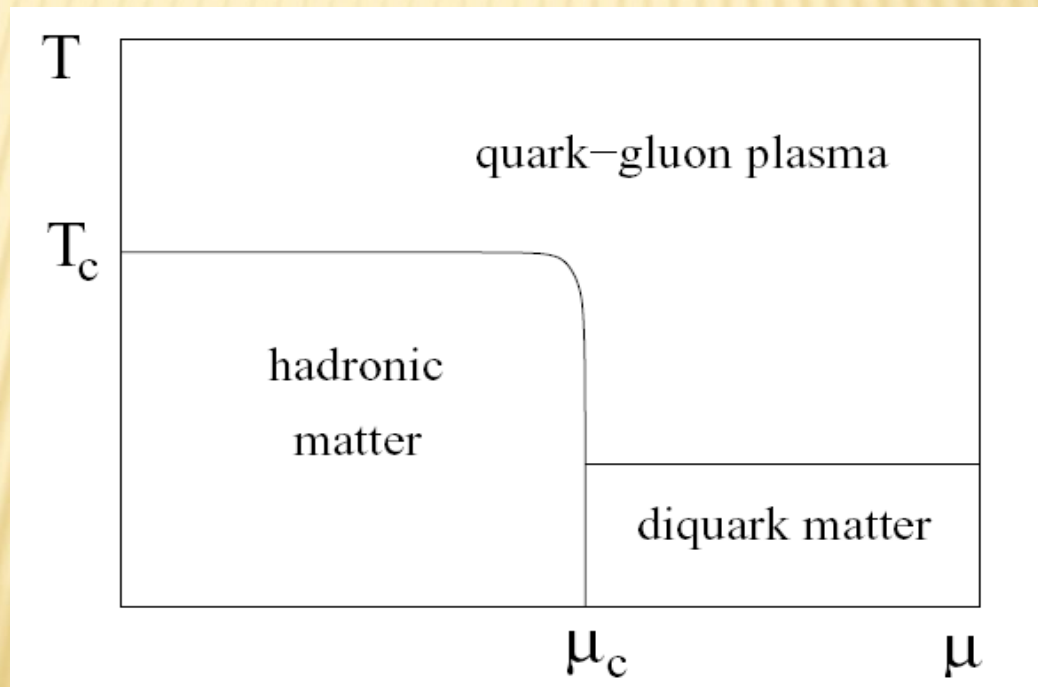
- ✗ What happens beyond  $T_c$  ? If hadrons are dimensionful bound states of more basic point-like entities hadronic matter consisting of these point-like constituents can therefore turn at high temperatures and/or densities into a plasma of the point-like constituents. This deconfining transition leads to a conducting (colour, for example) state and thus is the counterpart similar to the insulator-conductor transition in atomic matter.

Further transition phenomenon also expected from the behavior of atomic matter is a shift in the effective constituent mass. At  $T=0$  in vacuum quarks dress themselves with gluons to form the constituent quarks that make up hadrons. As a result, the bare quark mass is replaced by a constituent quark mass  $M_q \sim 300$  MeV and in a hot medium this dressing melts and  $M_q \neq m_q$ . Since the QCD Lagrangian for  $m_q=0$  is chirally symmetric  $M_q \neq 0$  should imply spontaneous chiral symmetry breaking. The melting  $M_q \rightarrow 0$  thus corresponds to chiral symmetry restoration. We shall see later on that in QCD, as in atomic physics, the shift of the constituent mass coincides with the onset of conductivity.



- ✘ So far, the “heating” of systems of low or vanishing baryon number density.  
The compression of baryonic matter at low temperature could result in another type of transition. This would set in if an attractive interaction between quarks in the deconfined baryon-rich phase results in the formation of colored bosonic diquark pairs, the counterpart of Cooper pairs in QCD. At sufficiently low temperature, these diquarks can then condense to form a color superconductor. Heating will dissociate the diquark pairs and turn the color superconductor into a normal color conductor.
- ✘ For a medium of quarks with color and flavor degrees of freedom, the diquark state can in fact consist of phases of different quantum number structures. It should be also noticed that for increasing baryon density the transition at low  $T$  could lead to an intermediate “quarkyonic” state in which baryons dissolve into quarks but mesons remain as confined states what is another interesting aspect of possible consistent theory.

Using baryochemical potential  $\mu$  as a measure for baryon density of system (i.e. for total number of baryons minus that of antibaryons per unit volume) we then expect the phase diagram of theory to have the general schematic form as shown. Given QCD as the fundamental theory of strong interactions we could use the QCD Lagrangian as dynamics input to derive the resulting thermodynamics of strongly interacting matter. For vanishing baryochemical potential  $\mu=0$  this can be evaluated with the lattice regularization.



Before turning to study QCD let us illustrate the transition from hadronic matter to quark-gluon plasma by very simple model. For ideal gas of massless pions, the pressure as function of the temperature is given by the Stefan-Boltzmann form

$$P_{\pi} = 3 \frac{\pi^2}{90} T^4$$

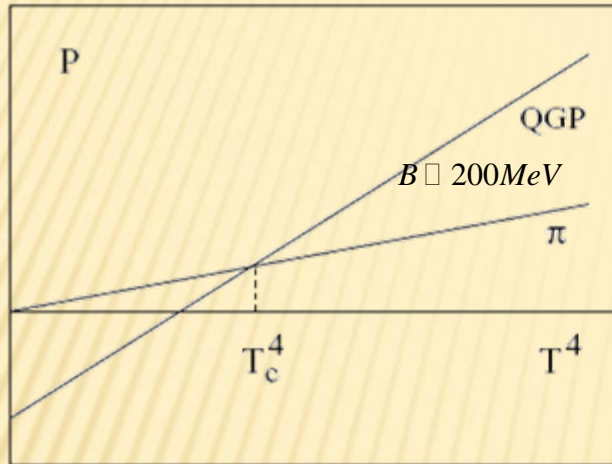
where factor 3 accounts for three charge states of the pion. The corresponding form for an ideal quark-gluon plasma with two flavors and three colors is

$$P_{qg} = \left\{ 2 \times 8 + \frac{7}{8} (3 \times 2 \times 2 \times 2) \right\} \frac{\pi^2}{90} T^4 - B = 37 \frac{\pi^2}{90} T^4 - B.$$

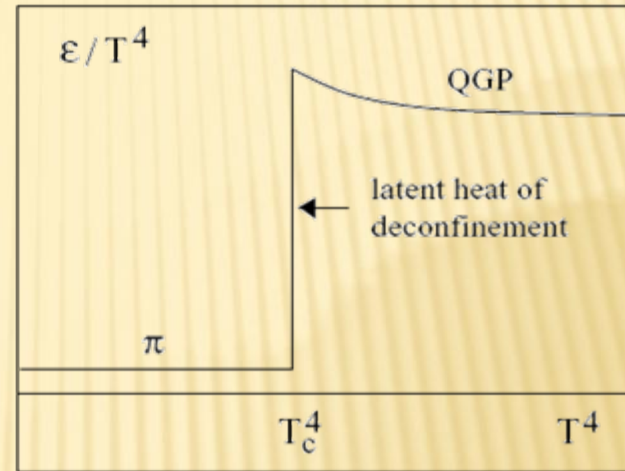
First term in curly brackets accounts for two spin and eight color degrees of freedom of gluons, the second for three color, two flavor, two spin and two particle-antiparticle degrees of freedom of quarks with 7/8 to obtain the correct statistics. Bag pressure  $B$  takes into account the (non-perturbative) difference between physical vacuum and ground state for colored quarks and gluons.



Since in thermodynamics a system chooses state of the lowest free energy and hence highest pressure compare the temperature behavior of both definitions.



(a)



(b)

This simple model thus leads to two-phase picture of strongly interacting matter with a hadronic phase up to **the temperature**

$$T_c = \left( \frac{45}{17\pi^2} \right)^{1/4} B^{1/4} \approx 0.72 B^{1/4}$$

and a quark-gluon plasma above this critical temperature. From hadron spectroscopy the bag pressure is given by  $B \approx 200 \text{ MeV}$  so that  $T_c \approx 150 \text{ MeV}$  as the deconfinement temperature.

**simple estimate remarkably close to the value obtained in lattice**

**QCD**

The energy densities of two phases of this model are given by

$$\varepsilon_{\pi} = \frac{\pi^2}{10} T^4 \quad \text{and} \quad \varepsilon_{qg} = 37 \frac{\pi^2}{30} T^4 + B.$$

By construction the transition is first order and the resulting temperature dependence is as shown. At  $T_c$  the energy density increases abruptly by the latent heat of deconfinement  $\Delta\varepsilon$ , its value is found to be

$$\Delta\varepsilon = \varepsilon_{qg}(T_c) - \varepsilon_{\pi}(T_c) = 4B,$$

so that it is determined completely by bag pressure measuring level difference between physical and colored vacua.

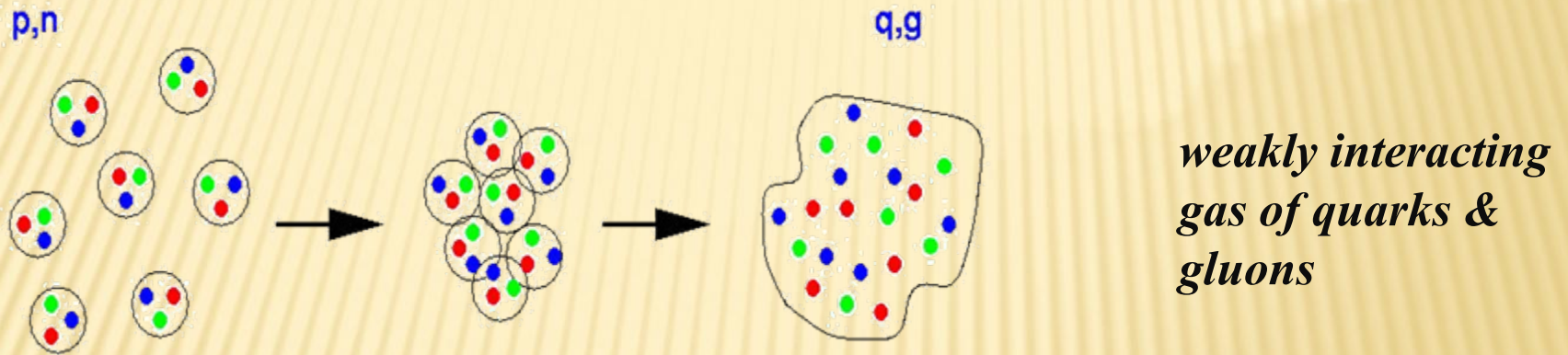
For an ideal gas of massless constituents the trace of energy-momentum tensor quite generally vanishes. Nevertheless, in this model of ideal plasma of massless quarks and gluons for  $T \geq T_c$  have

$$\varepsilon - 3P = 4B,$$

again specified by bag pressure and not zero. It is related to the so-called trace anomaly and indicates the dynamical generation of a dimensional scale; shall return to it and will find that this scale is set by vacuum expectation value of the gluon condensate.

## TAKE A DEEP BREATH ....

### ✗ What did we expect for QGP?



### ✗ What SHOULD we expect?

*quarks & gluons retain correlations,  
medium exhibits liquid properties*

***NB: the (quasi-)bound states are not your mother's hadrons!***





- A skier (quark?) is confined inside snow patches (hadrons?)

Temperature



- the skier can move further...a new phase develops

.. goes up



- a skier (quark?) can move freely over long distances...

.. this way

in QGP the coupling parameter could be

$$\Gamma = 2Cg^2/4\pi dT, \quad C - \text{Casimir invariant (} C=4/3 \text{ for quarks, } C=3 \text{ for gluons),}$$
$$d \sim 0.5 \text{ fm}, \quad T \sim 200 \text{ MeV}$$

take the coupling constant  $g \sim 2$  and 2 in the numerator comes from taking into account the magnetic interaction to addition to the static electric (Coulomb) interaction (the same magnitude supposed)

$$\Gamma \sim 1,5 \div 5$$

QGP in heavy ion collisions is a liquid rather than a gas

RHIC supports this crude estimate

**Does QCD show smthg similar?**

microscopic picture of phase transitions and QCD vacuum structure  
estimate of possible phenomena basing on instanton liquid model

A. Polyakov, **G 't Hooft**  
C. Callan, D. Dashen, **D. Gross**



collective phenomena observed at RHIC  
described by hydro allows to view QGP as **a near perfect liquid**

new idea: QGP at **RHIC** temperatures

$$T = (1 \div 2) T_c$$

seems to be in a strongly coupled regime  
**sQGP**

lattice QCD teaches: albeit quarks are deconfined at  $T > T_c$  they can't  
get  
separated,  $J/\Psi$  remains bound till  $T \sim 1,2 T_c$

there are a lot of bound states and resonance  
energy for separation of quarks close  $T_c$  is huge

**colour charges can't get separated until very high  
T and  
perturbative methods are hopeless**



# What is QCD?

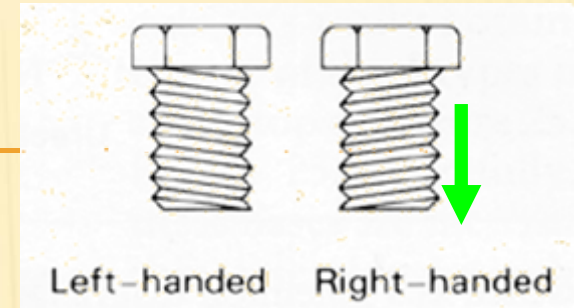
It is a field theory describing an interaction of quarks and gluons with Lagrangian

$$\mathcal{L} = -\frac{1}{4}G_{\mu\nu}^a G_{\mu\nu}^a + \sum_f \bar{q}_f^a (i\gamma_\mu D_\mu - m_f) q_f^a;$$

$$D_\mu = \partial_\mu - igA_\mu^a t^a$$

gluons

quarks



invariant at scale ( $x \rightarrow \lambda x$ ) and chiral left  $\longleftrightarrow$  right transformations in limit of massless quarks

both symmetries are broken by quantum effects

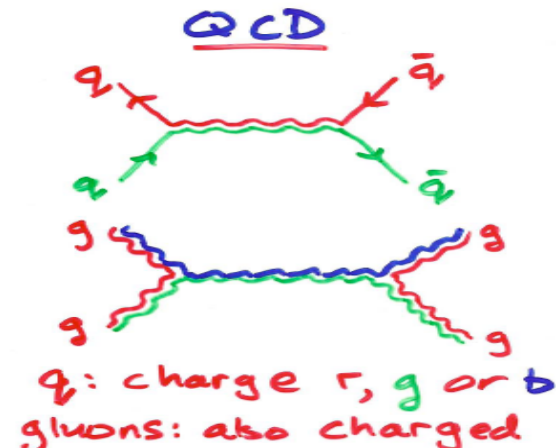
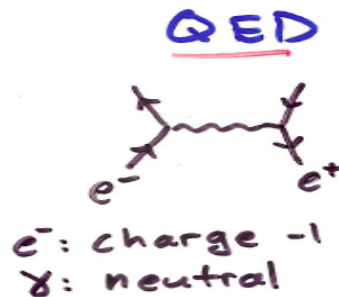
$$\partial^\mu s_\mu = \theta_\mu^\mu = m_f \bar{\psi} \psi_f + \frac{\beta(g)}{2g} G^{\mu\nu a} G_{\mu\nu}^a;$$

$$\partial^\mu J_{\mu 5} = 2m_f i \bar{\psi} \gamma_5 \psi_f - \frac{N_f g^2}{16\pi^2} G^{\mu\nu a} \tilde{G}_{\mu\nu}^a$$

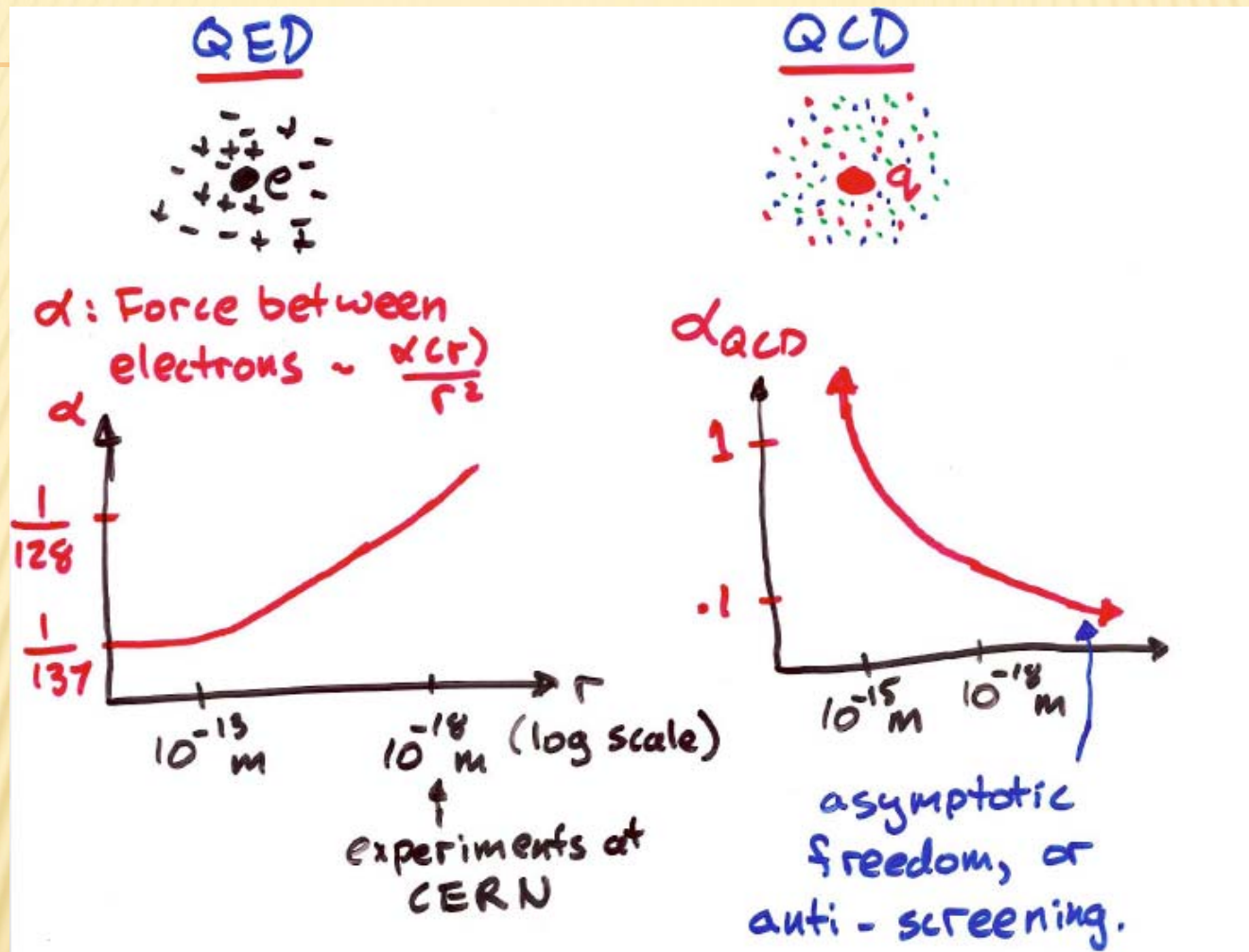
not much different Lagrangians of QCD and QED which describes the electron-photon interactions

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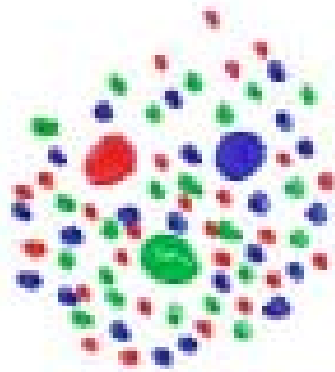
In quantum field theory the vacuum is a medium which can screen a charge



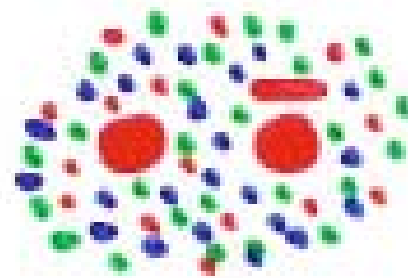
Coupling “constants” are not constant and depend on scale at which we probe quantum chromodynamics is different from quantum electrodynamics which is a theory of electrons and photons in presence of anti-screening and asymptotic freedom (Friedman, Kendall, and Taylor were able to see weakly interacting quarks because of this feature)

## What does QCD describes?

Today it is an experimental fact that in the world around us quarks and gluons appear only in colorless heavy aggregates protons, neutrons, pions, kaons, ...



**BARYON**



**MESON**

These hadrons are the quasi-particles of the QCD vacuum  
They make up everything from nuclei to neutron stars and  
thus most of the mass of us



## Why study QCD?

The only example we know of a strongly interacting gauge theory with quite understandable behavior at short distances (asymptotic freedom) at least.

Quasi-particles (vacuum excitations) which are hadrons do not look at all like the short distance quark and gluon degrees of freedom (deconfinement problem) and to study their properties and structure seems practical to get away from vacuum and

understand other phases of QCD and their quasi-particles.

At very high temperatures the QCD entropy wins over order and the symmetries of this phase should be

those of the QCD Lagrangian and asymptotic freedom tells that we must have weakly coupled quark and gluon quasi-particles.

We knew always that at  $1.5 - 2 T_c$  quantum chromodynamics is not yet weakly coupled (there are strong long distance magnetic interactions).

But lattice calculations demonstrated that above  $2T_c$  thermodynamic quantities do not change

more than 20%, there is a smooth crossover like ionization of a gas at  $T_c$  where hadrons “ionize”

and the order characterizing the QCD vacuum melts.

It allows us to believe a quasi-particle picture everywhere above the critical temperature

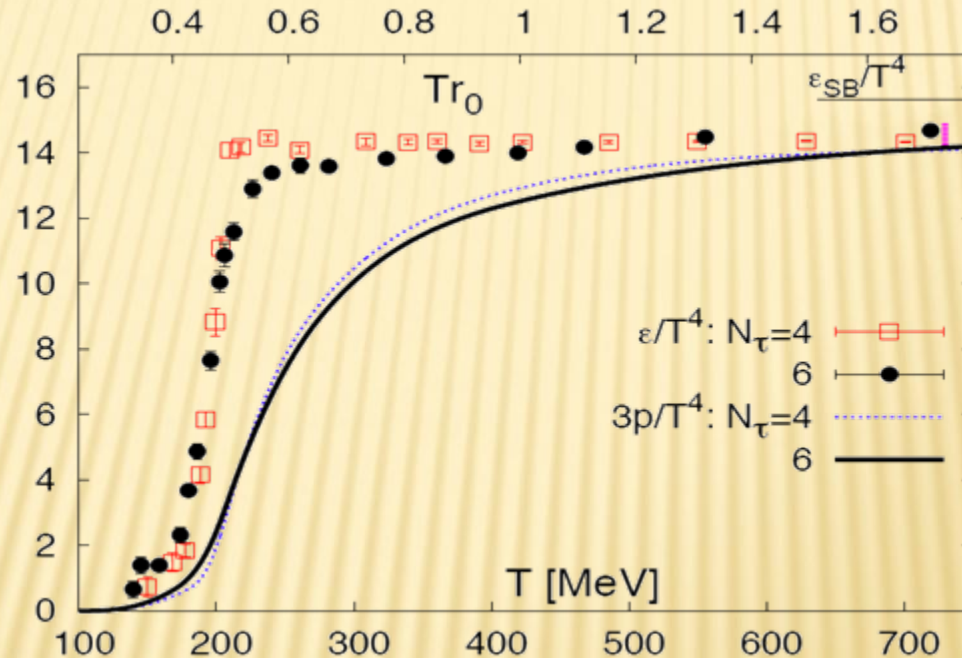
# Lattice Gauge Theory and Deconfinement:

**L is similar to a spin variable**

**=> Confinement-**

**Deconfinement transition**

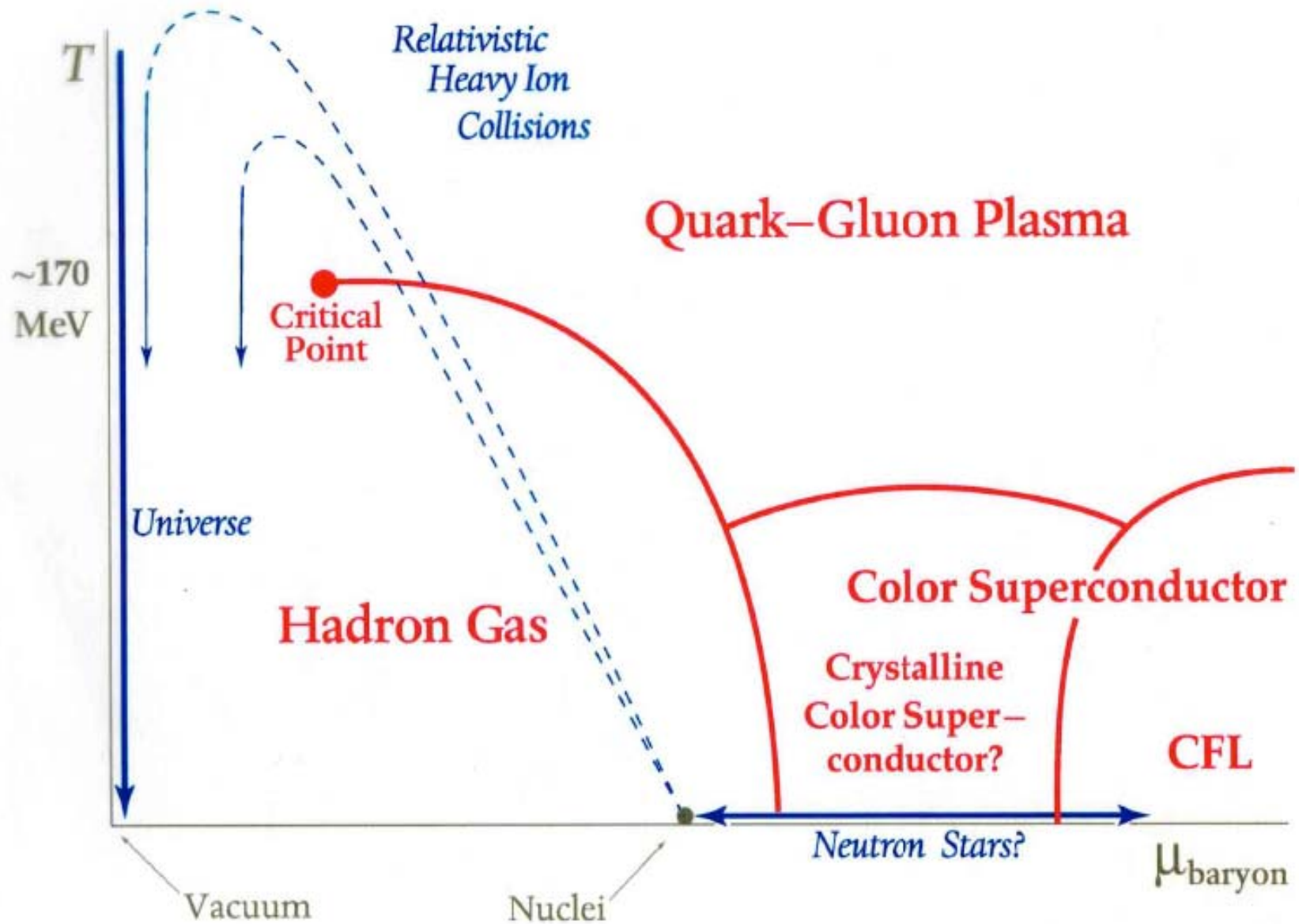
**Polyakov 1978    Susskind  
1979**



**Wuppertal, Bielefeld, BNL, MILC, Mumbai ...**

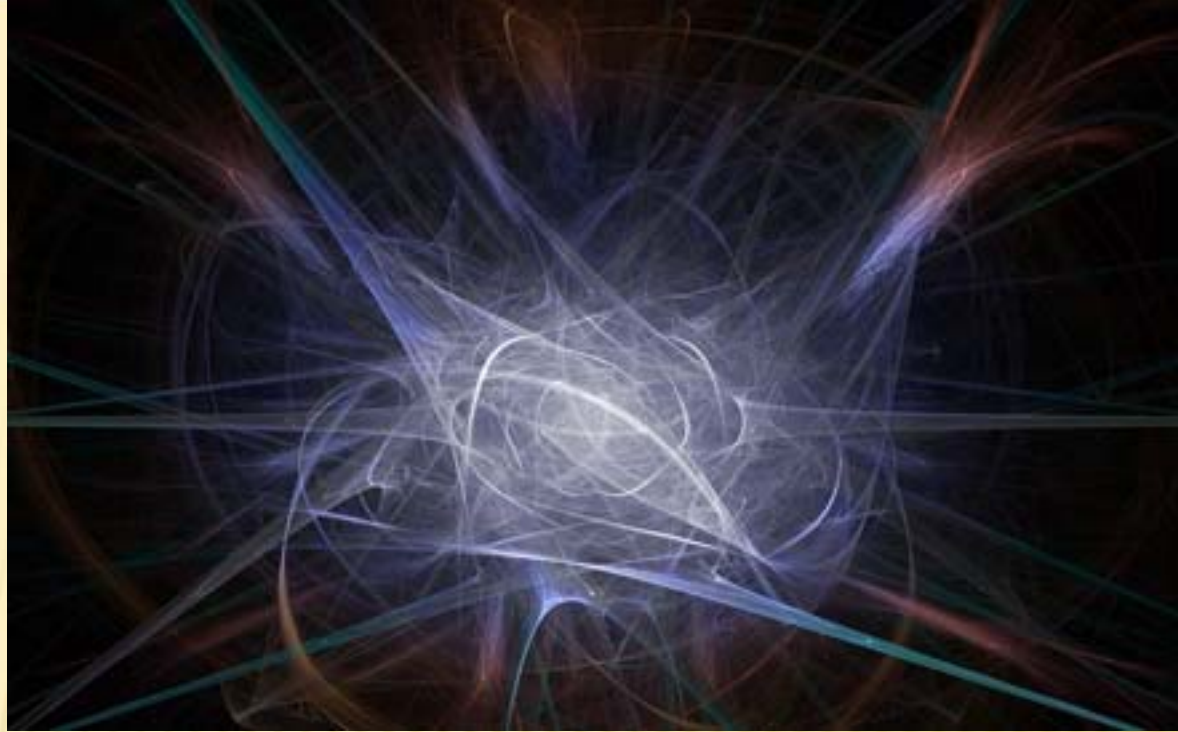
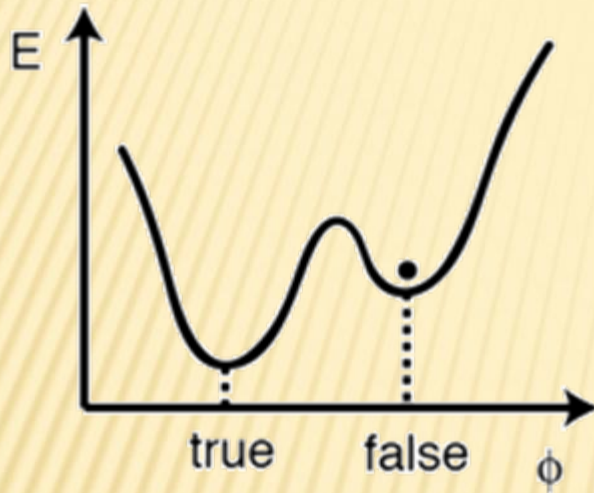
**First lattice computations at finite T; Kuti, Polonyi and Szlachanyi; McLerran and Svetitsky**

# EXPLORING *the* PHASES of QCD





**T.D. Lee**  
**Is our vacuum stable?**



Vacuum is not true  
ground state:  
Tunneling

Could hadronic collisions  
make such a transition?

**In this way one could temporarily restore broken symmetries of the physical vacuum and possibly create novel abnormal dense states of nuclear matter**

T. D. Lee and G. C. Wick

**Inflation of the universe from such  
transitions**

# **Origins of Ultrarelativistic Heavy Ion Collisions: Workshop on BeV Collisions of Heavy Ions: How and Why**

**Nov 29 - Dec 1 1974**

**Bear Mountain New York**

## **Introduction and Summary:**

**The history of physics teaches us that profound revolutions arise from a gradual perception that certain observations can be accommodated only by radical departures from current thinking. The workshop addressed itself to the intriguing question of the possible existence of a nuclear world quite different from the one we have learned to accept as familiar and stable.**

**Leon Lederman and Joseph Weneser**

**It would be interesting to explore new phenomena by distributing high energy or high nuclear density over a relatively large volume.**

**T. D. Lee**



Herodotus says,  
“Very few things happen at the right time...”



AGS-RHIC

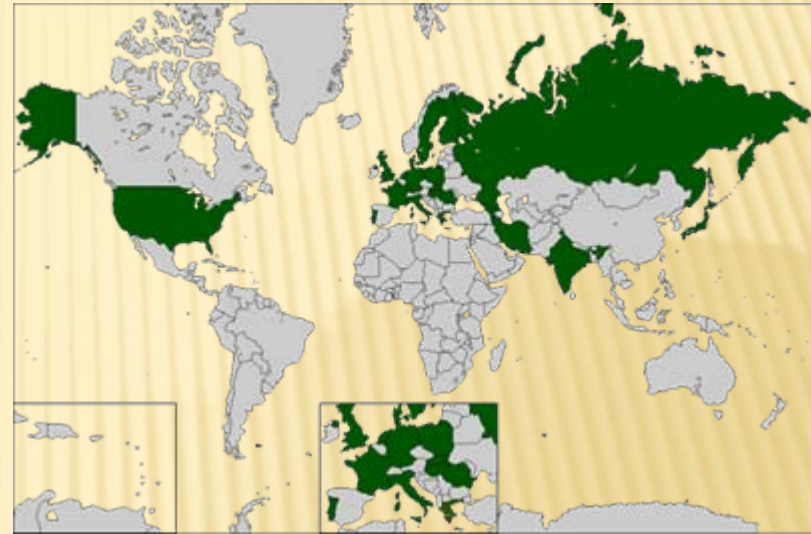
SPS-LHC



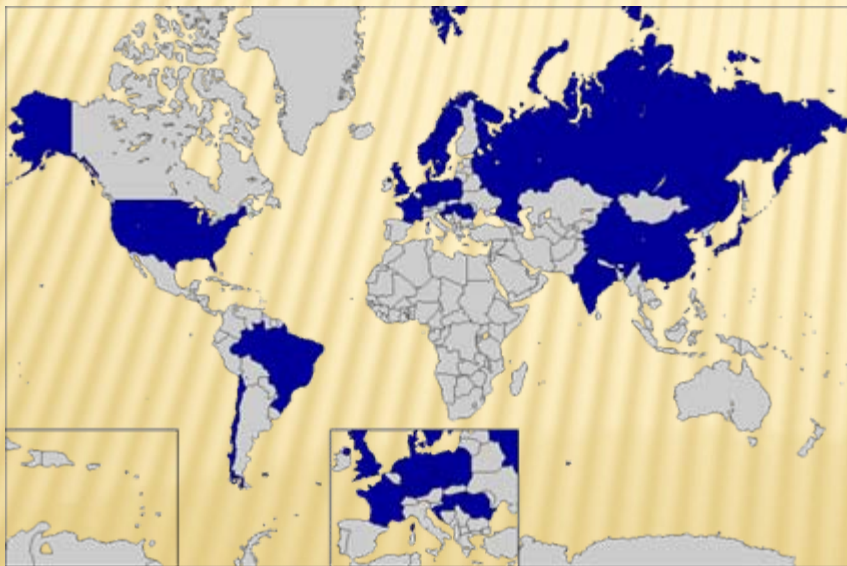
## From the Bevelac to the LHC:



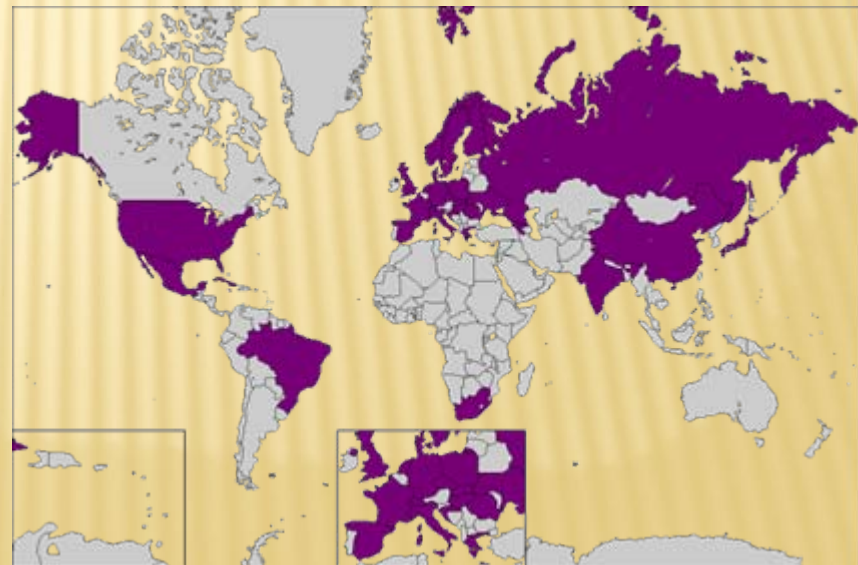
AGS



SPS



RHIC



Heavy Ions at LHC

Even a fully successful and quantitative model of heavy ion collisions will be of limited value to the broad scientific community if it does not bring us closer to answering the fundamental physics questions, such as:

*What is the mechanism of confinement?*

*What is the origin of chiral symmetry breaking?*

*What is the origin of mass?*